

國立嘉義大學 100 學年度  
生物機電工程學系碩士班招生考試試題

科目：工程數學（※禁止使用計算機）

1. Given a matrix  $A = \begin{bmatrix} 2 & 1 & 1 \\ 0 & 1 & 0 \\ 3 & 1 & 2 \end{bmatrix}$ .

- (a) Find the determinant of  $A$ . (10%)  
(b) Find the reduced row-echolen form of  $A$ , that is  $\text{rref}(A)=?$  (10%)  
(c) Find the rank of  $A$ . (5%)

2. Solve systems of differential equations: 
$$\begin{cases} \frac{dx}{dt} = 4x + 2y \\ \frac{dy}{dt} = 2x + y + 10 \end{cases} \quad (25\%)$$

3. A function  $y = y(x)$  satisfies that the 1<sup>st</sup>-order differential equation:

$$x \frac{dy}{dx} - 3x^3 + y = 0$$

- (a) Does the differential equation satisfy the “Condition of Exactness” ? (10%)  
(b) Solve the initial value problem given above for  $y(1) = 5$ . (10%)

4. Evaluate the followings:

(a) the Laplace transform of the piecewise function  $f(t) = \begin{cases} 2, & 0 \leq t < 2 \\ -2, & t \geq 2 \end{cases}$ . (10%)

(b) the inverse Laplace transform of  $G(s) = \frac{1}{s^2(s^2 + 9)}$ . (10%)

(c) the inverse Laplace transform of  $H(s) = \ln \frac{s^2 + 4}{s^2}$ . (10%)