For a system with output *y* and input *r* described by the following equation:

$$
\frac{d^5 y}{dt^5} + 2\frac{d^4 y}{dt^4} + 8\frac{d^3 y}{dt^3} + 11\frac{d^2 y}{dt^2} + 16\frac{dy}{dt} + 12y = 5\frac{d^2 r}{dt^2} + 4\frac{dr}{dt} + 7r
$$

- (a) Find the transfer function of the system.  $(5\%)$
- (b) Determine the stability of the system using the Routh-Hurwiz criterion. (10%)
- (c) Write down an equivalent state space representation. (5%)
- (d) Sketch the state variable diagram. (5%)

(a) Determine the closed-loop transfer function from  $R(s)$  to  $Y(s)$ . (5%) (b) Draw the root locus of the system with as a varying parameter. (15%)

(c) Determine the value of for the system to be critically damped.  $(5%)$ 

The block diagram of a control system is given in Figure 2.



Figure 2

- (a) The individual responses of two linear control system elements A and B each to a unit step input are given in Figure 3a. Use the response data to estimate transfer functions for A and B. (15%)
- (b) The elements A and B are now placed in a feedback control system, as shown in Figure 3b, in which the proportional gain constant K is adjustable. Derive an expression for the closed-loop transfer function and determine the range of values of K for which the system will be stable. (10%)

Note: Values of peak overshoot for a second order system are given in Table 1.

Table 1 Peak overshoot for second order system

		◡.◡	◡.◡		
$\%$ overshoot	ັ				





Derive the state variable equations (10%) for a DC motor system (Figure 4) that has a constant field voltage  $E_F$ , an applied armature voltage  $e_a(t)$ , and a load torque  $\tau_L(t)$ . Also obtain the transfer function (5%) with  $\omega_L$  as the output, and determine the steady-state angular velocities corresponding to the following sets of inputs:

(1)  $e_a(t) = E$ ,  $\tau_L(t) = 0$  (5%) and (2)  $e_a(t) = 0$ ,  $\tau_L(t) = L$  (5%).



Figure 4