

# 國立嘉義大學九十三年學年度

## 光電暨固態電子研究所碩士班招生考試試題

### 科目：電磁學

- 一、 Two infinite insulated conducting planes maintained at potentials 0 and  $V_0$  form a wedge-shaped configuration, as shown in Fig. 1. Determine the potential distributions for the regions:
- ( a )  $0 < \phi < \alpha$ . (10%)
  - ( b )  $\alpha < \phi < 2\pi$ . (10%)

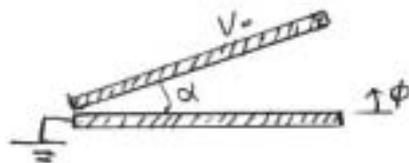


Fig. 1

- 二、 A capacitor consists of two concentric spherical shells of radii  $R_i$  and  $R_o$ . The space between them is filled with a dielectric of relative permittivity  $\epsilon_r$  from  $R_i$  to  $b$  ( $R_i < b < R_o$ ) and another dielectric of relative permittivity  $3\epsilon_r$  from  $b$  to  $R_o$ . Determine :
- ( a )  $\vec{E}$  and  $\vec{D}$  everywhere ( $R < R_i$ ,  $R_i < R < b$ ,  $b < R < R_o$ ,  $R > R_o$ ) in terms of an applied voltage  $V$ . (15%)
  - ( b ) the capacitance. (5%)
- 三、 A current  $I$  flows down a long straight wire of radius  $a$ . If the wire is made of linear material (copper, say, or aluminum) with susceptibility  $x_m$ , and the current is distributed uniformly,
- ( a ) What is the magnetic field at a distance  $s$  from the axis? (6%)
  - ( b ) Find all the bound currents. (8%)
  - ( c ) What is the net bound current flowing down the wire? (6%)
- 四、 An alternating current  $I = I_0 \cos(\omega t)$  flows down a long straight wire, and returns along a coaxial conducting tube of radius  $a$ .
- ( a ) In what direction does the induced electric field point (radial, circumferential, or longitudinal) ? (4%)
  - ( b ) Assuming that the field goes to zero as  $s \rightarrow \infty$ , find  $\vec{E}(s, t)$ . (6%)
  - ( c ) Integrate the displacement current density  $\vec{J}_d$  to get the total displacement current  $\vec{I}_d$ . (10%)
- 五、 From the point of view of electromagnetics, the power transmitted by a lossless coaxial cable can be considered in terms of the Poynting vector inside the dielectric medium between the inner conductor and the outer sheath. Assuming that a d-c voltage  $V_0$  applied between the inner conductor (of radius  $a$ ) and the outer sheath (of inner radius  $b$ ) causes a current  $I$  to flow to a load resistance, verify that the integration of the Poynting vector over the cross-sectional area of the dielectric medium equals the power  $V_0 I$  that is transmitted to the load. (20%)